

*New Progress on FDC project*  
*- Automatic deduction renormalization counter term*

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- It is well known that precision theoretical description on high energy phenomenology must be achieved.
- Therefore, higher-order perturbative calculations in QFT for SM are required for signal and background.
- FDC project is aimed at automatic calculation on these calculation and already can do next-leading-order(NLO) calculation automatically.
- Based on FDC, there are already many hard works been achieved in last 8 years.
- Recent progress for FDC project will be introduced in this talk.

# Brief Introduction to FDC package

Feynman Diagram Calculation(FDC).

This first version of FDC was presented at AIHENP93 workshop,1993.

FDC Homepage::

[http://www.ihep.ac.cn/lunwen/wjx/public\\_html/index.html](http://www.ihep.ac.cn/lunwen/wjx/public_html/index.html)

*FDC-LOOP*

FDC-PWA

FDC-EMT

FDC-SM-and-Many-Extensions

FDC-NRQCD

FDC-MSSM

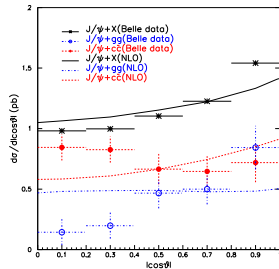
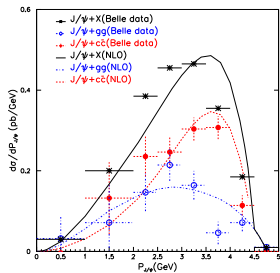
Written in REDUCE,  
RLISP,C++.  
To generate Fortran

Event Generator

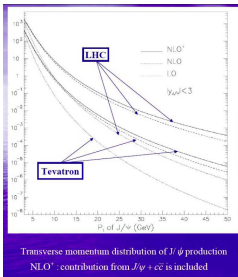
- The results are obtained analytically.
- Two ways to generate square of amplitude:
- Automatically phase space treatment
- To automatically construct the Lagrangian and deduce the Feynman rules for SM, MSSM
- First version of “FDC-LOOP” was completed by the end of 2007, used and improved since then.
- Many work on QCD correction are finished and published.
- First version of FDC-PWA was completed on 2001 and improved 2003, used by BES experimental group for partial-wave analysis

# The calculations by using FDC-loop in last 8 years

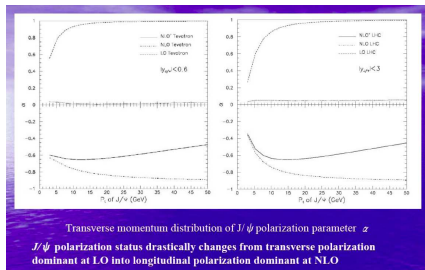
- Our work concentrate on QCD correction to heavy quarkonium production and polarization in B-factory, z boson decay,  $\Upsilon$  decay, HERA, Tevatron, LHC.
- It is found that that QCD corrections to these processes are very important.



Momentum distribution of  $J/\psi$  for  $e^+e^- \rightarrow J/\psi + gg$  at QCD NLO. PRL102, (2009) B. Gong and J. X. Wang



Transverse momentum distribution of  $J/\psi$  production  
NLO\* contribution from  $J/\psi + c\bar{c}$  is included



Transverse momentum distribution of  $J/\psi$  polarization parameter  $z$   
 $J/\psi$  polarization status drastically changes from transverse polarization  
dominant at LO into longitudinal polarization dominant at NLO

$P_T$  distribution of  $J/\psi$  polarization at QCD NLO. PRL100,232001 (2008), B. Gong and J. X. Wang

# QCD Correction to prompt $J/\psi$ ( $^3S_1^1, ^1S_0^8, ^3S_1^8, ^3P_J^8$ ) polarization

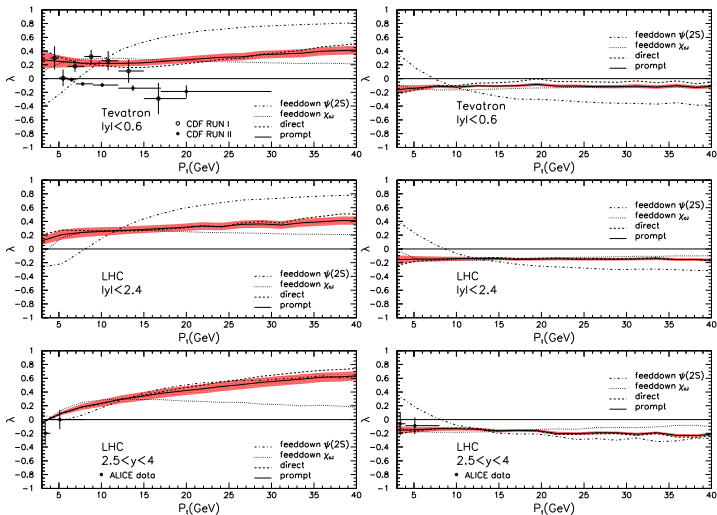
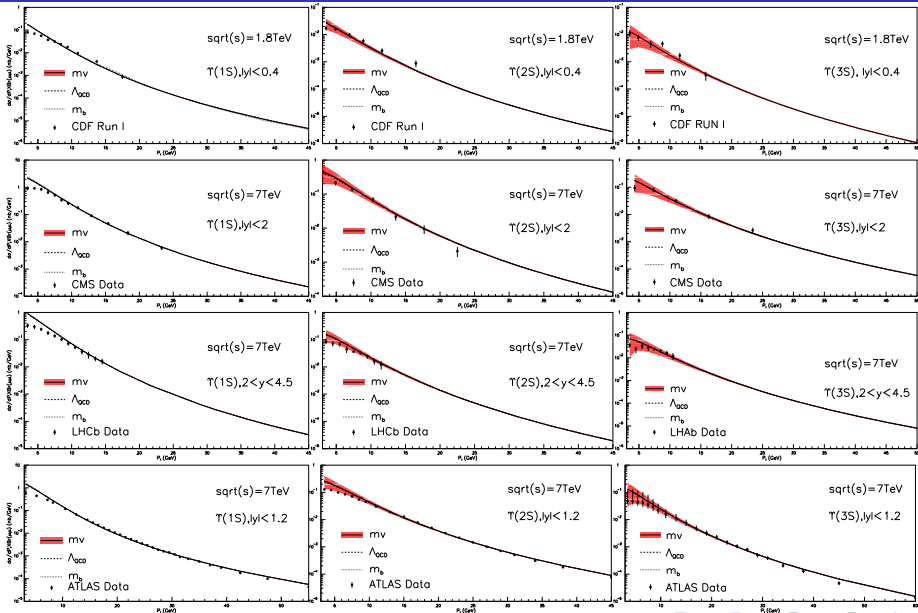


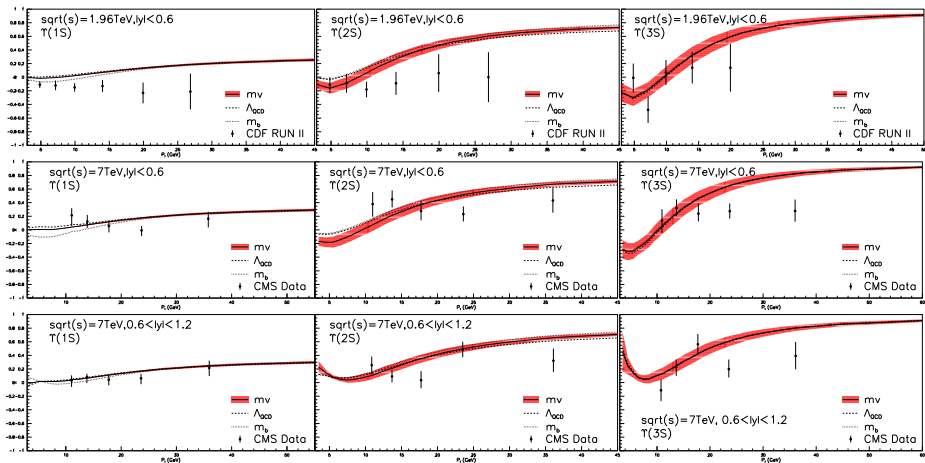
Figure: Polarization parameter  $\lambda$  of prompt  $J/\psi$  hadroproduction in helicity(left) and CS(right) frames.

# QCD Correction to $\Upsilon(1S, 2S, 3S)$ production





# QCD Correction to $\Upsilon(1S, 2S, 3S)$ polarization



PRL 112, 032001, 2014, by Bin Gong, Lu-Ping Wan, Jian-Xiong Wang and Hong-Fei Zhang  
**Figure:** Polarization parameter  $\lambda$  of prompt  $\Upsilon(1S, 2S, 3S)$  hadroproduction in helicity frame

# Recent Progress in FDC project

- New algorithm to construct and triangulate convex polyhedral cone and its application in higher order perturbative QFT calculation (I presented the talk on High1-2016 workshop)
- automatic counter terms generation , automatic calculation of renormalization constant (This talk on High1-2017 workshop)

# Tree-level Lagrangian construction and Feynman rules generation

- 1994, Standard Model, 3 gauge group, 3 generation quark and leptons, more than 100 interaction vertices
- 2000, MSSM, 3 gauge group and supersymmetry, 3 generation quark and leptons with their super partners, more than 5000 interaction vertices
- 2008, QCD one-loop counter term input by hand.

# One-loop counter terms generation in last year

To construct counter terms and calculation all the renormalization constants for QCD or electro-weak one-loop renormalization.

- Very simple description input for first principle model with  $SU(n)$  gauge symmetry, such as the Standard Model, two-higgs doublet model, ....
- Easy to add different matter fields
- Different gauge can be easily chosen, such as unitary gauge, Feynman-tohft gauge, R-ksi Gauge, Landau gauge, ...
- Different renormalization scheme, such as Keyto-scheme, European-scheme, On-shell or  $\overline{MS}$ -bar scheme for QCD renormalization choice.
- For MSSM one-loop renormalization is still under construction.
- Two-loop counter terms generation are under construction

# European scheme (gauge-symmetric scheme)

## The on-shell subtraction conditions

- 1  $R_e \hat{\Sigma}(M_w^2) = R_e \hat{\Sigma}^{zz}(M_z^2) = R_e \hat{\Sigma}^f(\not{p} = m_f) = 0$
- 2  $\hat{\Gamma}_\mu^{\gamma ee}(k^2 = 0, \not{p} = \not{q} = m_e) = ie\gamma_\mu$
- 3  $\hat{\Gamma}^{\gamma z}(0) = 0$
- 4  $\frac{\partial \hat{\Gamma}^{\gamma\gamma}}{\partial k^2}(0) = 0$
- 5  $\lim_{\not{k} \rightarrow m_-} \frac{1}{\not{k} - m_-} \hat{\Gamma}^f(k) \mu_-(k) = 0$   
(if  $\mu_-$  is the wave function for  $l_3 = -1/2$  particle.)

The last condition is formulated for charged leptons and quarks with  $l_3 = -1/2$ . Thus we could derive the renormalization constant  $Z_L$  and  $Z_R^-$ . In the same time, the  $Z_L$  also determines the  $l_3 = +1/2$  (in this scheme, we keep the  $Su(2)$  gauge symmetry, so for  $Su(2)$  doublet we must have same renormalization constant). For above case the residue of  $l_3 = +1/2$  quark and neutrino propagator is not equal to 1.

## European scheme (gauge-symmetric scheme)

So the  $\gamma_\mu$  term and  $\gamma_\mu\gamma_5$  term in  $S_F^f(k)$  is

$$S_{\gamma_\mu}^f(k) = \frac{i}{\not{k} - m_f} \not{k} \Gamma_V^f(k^2) \frac{i}{\not{k} - m_f}$$

$$S_{\gamma_5}^f(k) = \frac{i}{\not{k} - m_f} \not{k} \gamma_5 \Gamma_A^f(k^2) \frac{i}{\not{k} - m_f}$$

We write them in a simplifying form i.e.

$$S_{\gamma_5}^f(k) = \frac{1}{(k^2 - m_f^2)^2} (k^2 - m_f^2) \not{k} \Gamma_A^f(k^2)$$

$$S_{\gamma_\mu}^f(k) = \frac{1}{(k^2 - m_f^2)^2} (\not{k} + m_f)(\not{k} + m_f) \not{k} \gamma_5 \Gamma_V^f(k^2)$$

Compare the two equations we find that  $S_5^f(k)$  there is a  $k^2 - m_f^2$  factor.

That's why we say the Taylor expansion at  $k^2 = m^2$  of  $\gamma_5$  term has no zero order term, it begins with one order.

# The renormalization of mixing fields in electroweak

It would be different for mixing fields when we do renormalization.

for example:

$$\begin{pmatrix} Z_\mu \\ A_\mu \end{pmatrix} = \begin{pmatrix} \cos\theta_w & -\sin\theta_w \\ \sin\theta_w & \cos\theta_w \end{pmatrix} \begin{pmatrix} W_\mu^3 \\ B_\mu \end{pmatrix} \quad (1)$$

We do renormalization as follow:

$$\begin{pmatrix} Z_\mu \\ A_\mu \end{pmatrix}_0 = \begin{pmatrix} 1 + \frac{1}{2}\delta Z_Z Z & \frac{1}{2}\delta Z_Z A \\ \frac{1}{2}\delta Z_A Z & 1 + \frac{1}{2}\delta Z_A A \end{pmatrix} \begin{pmatrix} Z_\mu \\ A_\mu \end{pmatrix} \quad (2)$$

Inverting the matrix, we obtain the renormalized propagator as

$$\begin{aligned}
& (i\hat{D}_{WA}(q^2))_{\mu\nu} \\
= & -g_{\mu\nu} \left( \begin{array}{cc} \frac{1}{q^2 - M_Z^2 - \hat{\Pi}_{ZZ}} & \frac{1}{q^2 - m_\gamma^2} \frac{\hat{\Pi}_{AZ}}{q^2 - M_Z^2 - iIm\hat{\Pi}_{ZZ}} \\ \frac{1}{q^2 - m_\gamma^2} \frac{\hat{\Pi}_{AZ}}{q^2 - M_Z^2 - iIm\hat{\Pi}_{ZZ}} & \frac{1}{q^2 - m_\gamma^2 - \hat{\Pi}_{AA}} \end{array} \right) \\
& -i \frac{q_\mu q_\nu}{q^2} \left( \begin{array}{cc} \frac{1}{q^2 - M_Z^2 - \hat{\Pi}_{ZZ}} \frac{q^2(\xi_Z - 1) + \xi_Z \hat{\Pi}_{ZZ}^L}{q^2 - \xi_Z M_Z^2 - \xi_Z(\hat{\Pi}_{ZZ}^L + \hat{\Pi}_{ZZ})} & \frac{1}{q^2 - m_\gamma^2} \frac{\hat{\Pi}_{AZ}^L}{q^2 - M_Z^2 - iIm\hat{\Pi}_{ZZ}} \\ \frac{1}{q^2 - m_\gamma^2} \frac{\hat{\Pi}_{AZ}^L}{q^2 - M_Z^2 - iIm\hat{\Pi}_{ZZ}} & \frac{1}{q^2 - m_\gamma^2} \frac{q^2(\xi_\gamma - 1) + \xi_\gamma \hat{\Pi}_{AA}^L}{q^2 - \xi_\gamma m_\gamma^2 - \xi_\gamma(\hat{\Pi}_{AA}^L + \hat{\Pi}_{AA})} \end{array} \right), \tag{c.12}
\end{aligned}$$

which becomes to one-loop order

$$\begin{aligned}
& (i\hat{D}_{WA}(q^2))_{\mu\nu} \\
= & -ig_{\mu\nu} \left( \begin{array}{cc} \frac{1}{q^2 - M_Z^2} & 0 \\ 0 & \frac{1}{q^2 - m_\gamma^2} \end{array} \right) \\
& -iq_\mu q_\nu \left( \begin{array}{cc} \frac{\xi_Z - 1}{(q^2 - M_Z^2)(q^2 - \xi_Z M_Z^2)} & 0 \\ 0 & \frac{\xi_\gamma - 1}{(q^2 - m_\gamma^2)(q^2 - \xi_\gamma m_\gamma^2)} \end{array} \right) \\
& -ig_{\mu\nu} \left( \begin{array}{cc} \frac{1}{q^2 - M_Z^2} \hat{\Pi}_{ZZ} \frac{1}{q^2 - M_Z^2} & \frac{1}{q^2 - m_\gamma^2} \hat{\Pi}_{AZ} \frac{1}{q^2 - M_Z^2} \\ \frac{1}{q^2 - m_\gamma^2} \hat{\Pi}_{AZ} \frac{1}{q^2 - M_Z^2} & \frac{1}{q^2 - m_\gamma^2} \hat{\Pi}_{AA} \frac{1}{q^2 - m_\gamma^2} \end{array} \right) \\
& -i \frac{q_\mu q_\nu}{q^2} \left( \begin{array}{cc} C_{ZZ} \hat{\Pi}_{ZZ} + \xi_Z^2 \frac{\hat{\Pi}_{ZZ}^L}{(q^2 - \xi_Z M_Z^2)^2} & \frac{1}{q^2 - m_\gamma^2} \hat{\Pi}_{AZ}^L \frac{1}{q^2 - M_Z^2} \\ \frac{1}{q^2 - m_\gamma^2} \hat{\Pi}_{AZ}^L \frac{1}{q^2 - M_Z^2} & C_{\gamma\gamma} \hat{\Pi}_{AA} + \xi_\gamma^2 \frac{\hat{\Pi}_{AA}^L}{(q^2 - \xi_\gamma m_\gamma^2)^2} \end{array} \right), \tag{c.13}
\end{aligned}$$



# Input file for Standard Model at electroweak NLO

```

%----- Gauge fields -----
gaugefields:=
%No. Name SU(n) notation coupling breaking
'(1 u 1 b g1 yes )
(2 su 2 a g yes )
(3 su 3 gs g3 no )}$
%----- Matter fields -----
matterinput:={{name, 2*spin, chiral, 1, 2, 3},
{hig, 0, rl, 1, 2, 0},
{el, 1, l, -1, 2, 0},
{er, 1, r, -2, 0, 0},
{q1l, 1, l, 1/3, 2, 3},
{q1dr, 1, r, -2/3, 0, 3},
{q1ur, 1, r, 4/3, 0, 3}}$
gauge_boson_redefine:={
a(1,~v) => (w(1,v)+w(-1,v))/2**0.5,
a(2,~v) => (w(-1,v)-w(1,v))/2**0.5/i,
a(3,~v) => z(0,v), b(~v) => p(0,v)};
vancumexpectation:='(hig v0));

% name n_group 1_componet 2_componet ...
mdefl:={ {hig, 2, xx2, (v0+h0-i*xx3)/2**0.5},
{el, 2, nue, ef },
{er, 2, ef },
{q1l, 2, qu, qd },
{q1dr, 2, qd },
{q1ur, 2, qu }}$

realfamily:='( q1l q2l q3l) (q1dr q2dr q3dr)
(q1ur q2ur q3ur) (qu qc qt) (qd qs qb) (el mul tau)
(er mur taur) (ef mu tau) (nue numu nut));

phymass:={{w, wm}, {z, zm}, {p, 0}, {h0, hm},
{ef, fme}, {nue, 0},{mu, fmmu},{numu, 0},{tau, fmtau},
{nut, 0},{qd, fmd}, {qu, fmu},{qs, fms}, {qc, fmc},
{qb, fmb}, {qt, fmt}}$

phyinput:={g3,g,theta,wm, hm,fme, fmmu,fmtau,fmd,
fmu,fms, fmc,fmb, fmt}$

construles:={ g1=>g*sin(theta)/cos(theta)};

exprimment_easy_list:={
{g, replaceby, ge, -i*ge*gg(l,v), {p,ef,ef}},
{theta, replaceby, zm} };

charge_def:=tp(2,3)+tp(1,1)/2;

renormalization:='before_broken; %European scheme
%renormalization:='after_broken; %Kyoto scheme

%ms_list:='(g3 );

symbolic(rform:='(1 2 ));
symbolic(rloop:='((g . 2)));

```

## Generated File: "gauge\_fix\_term" Can be used to choose different Gauge

```
fy!={
{p, ksi1, sin(theta)*pd(a(3,v),v)+cos(theta)*pd(b(v),v),sin(theta)*(mutiplet(-1,2,hig,2,xx2(-1),
(h0(0)+xx3(0)*i)/sqrt(2))*tp(1,2,2,3)*mutiplet(1,2,hig,2,0,v0/sqrt(2))*g*i-mutiplet(1,2,hig,2,0,v0
/sqrt(2))*tp(1,2,2,3)*mutiplet(1,2,hig,2,xx2(1),(h0(0)-xx3(0)*i)/sqrt(2))*g*i/
2+cos(theta)*(mutiplet(-1,2,hig,2,xx2(-1),(h0(0)+xx3(0)*i)/sqrt(2))*mutiplet(1,2,hig,2,0,v0/
sqrt(2))*g1*i-mutiplet(-1,2,hig,2,0,
v0/sqrt(2))*mutiplet(1,2,hig,2,xx2(1),(h0(0)-xx3(0)*i)/sqrt(2))*g1*i)/2,
gh(-1,2,3)*sin(theta)+gh(-1,1)*cos(theta)},

{z, ksi2, cos(theta)*pd(a(3,v),v)+(-sin(theta))*pd(b(v),v),cos(theta)*(mutiplet(-1,2,hig,2,xx2(-1),
(h0(0)
+xx3(0)*i)/sqrt(2))*tp(1,2,2,3)*mutiplet(1,2,hig,2,0,v0/sqrt(2))*g*i-mutiplet(-1,2,hig,2,0,v0/sqrt(2))*
tp(1,2,2,3)*mutiplet(1,2,hig,2,xx2(1),(h0(0)-xx3(0)*i)/sqrt(2))*g*i)/2+(-sin(theta))*(mutiplet(-1,2,hig,
2,xx2(-1),(h0(0)+xx3(0)*i)/sqrt(2))*mutiplet(1,2,hig,2,0,v0/sqrt(2))*g1*i-mutiplet(-1,2,hig,2,0,v0
/sqrt(2))*mutiplet(1,2,hig,2,xx2(1),(h0(0)-xx3(0)*i)/sqrt(2))*g1*i)/2,
gh(-1,2,3)*cos(theta)-gh(-1,1)*sin(theta)},

{a(1), ksi3, pd(a(1,v),v),(mutiplet(-1,2,hig,2,xx2(-1),(h0(0)+xx3(0)*i)/sqrt(2))*tp(1,2,2,1)*
mutiplet(1,2,hig,2,0,v0/sqrt(2))*g*i-mutiplet(-1,2,hig,2,0,v0/sqrt(2))*tp(1,2,2,1)*mutiplet(1,2,hig,2,
xx2(1),(h0(0)-xx3(0)*i)/sqrt(2))*g*i)/2, gh(-1,2,1)},

{a(2), ksi3, pd(a(2,v),v),(mutiplet(-1,2,hig,2,xx2(-1),(h0(0)+xx3(0)*i)/
sqrt(2))*tp(1,2,2,2)*mutiplet(1,2,
hig,2,0,v0/sqrt(2))*g*i-mutiplet(-1,2,hig,2,0,v0/sqrt(2))*tp(1,2,2,2)*mutiplet(1,2,hig,2,xx2(1),
(h0(0)-xx3(0)*i)/sqrt(2))*g*i)/2, gh(-1,2,2)},

{gs(ic10), ksi4 ,pd(gs(ic10,v),v),0, gsg(-1,ic10)}}$

r_ksi_value:=( ksi1 . 1) (ksi2 . 1) (ksi3 . 1) (ksi4 . 1))$ %Default Feynman-tohoft gauge
```

## Generated File: "gauge\_fix\_term" Can be used to choose different Gauge

```
fy!={
{p, ksi1, sin(theta)*pd(a(3,v),v)+cos(theta)*pd(b(v),v),sin(theta)*(mutiplet(-1,2,hig,2,xx2(-1),
(h0(0)+xx3(0)*i)/sqrt(2))*tp(1,2,2,3)*mutiplet(1,2,hig,2,0,v0/sqrt(2))*g*i-mutiplet(1,2,hig,2,0,v0
/sqrt(2))*tp(1,2,2,3)*mutiplet(1,2,hig,2,xx2(1),(h0(0)-xx3(0)*i)/sqrt(2))*g*i/
2+cos(theta)*(mutiplet(-1,2,hig,2,xx2(-1),(h0(0)+xx3(0)*i)/sqrt(2))*mutiplet(1,2,hig,2,0,v0/
sqrt(2))*g1*i-mutiplet(-1,2,hig,2,0,
v0/sqrt(2))*mutiplet(1,2,hig,2,xx2(1),(h0(0)-xx3(0)*i)/sqrt(2))*g1*i)/2,
gh(-1,2,3)*sin(theta)+gh(-1,1)*cos(theta)},

{z, ksi2, cos(theta)*pd(a(3,v),v)+(-sin(theta))*pd(b(v),v),cos(theta)*(mutiplet(-1,2,hig,2,xx2(-1),
(h0(0)
+xx3(0)*i)/sqrt(2))*tp(1,2,2,3)*mutiplet(1,2,hig,2,0,v0/sqrt(2))*g*i-mutiplet(-1,2,hig,2,0,v0/sqrt(2))*
tp(1,2,2,3)*mutiplet(1,2,hig,2,xx2(1),(h0(0)-xx3(0)*i)/sqrt(2))*g*i)/2+(-sin(theta))*(mutiplet(-1,2,hig,
2,xx2(-1),(h0(0)+xx3(0)*i)/sqrt(2))*mutiplet(1,2,hig,2,0,v0/sqrt(2))*g1*i-mutiplet(-1,2,hig,2,0,v0
/sqrt(2))*mutiplet(1,2,hig,2,xx2(1),(h0(0)-xx3(0)*i)/sqrt(2))*g1*i)/2,
gh(-1,2,3)*cos(theta)-gh(-1,1)*sin(theta)},

{a(1), ksi3, pd(a(1,v),v),(mutiplet(-1,2,hig,2,xx2(-1),(h0(0)+xx3(0)*i)/sqrt(2))*tp(1,2,2,1)*
mutiplet(1,2,hig,2,0,v0/sqrt(2))*g*i-mutiplet(-1,2,hig,2,0,v0/sqrt(2))*tp(1,2,2,1)*mutiplet(1,2,hig,2,
xx2(1),(h0(0)-xx3(0)*i)/sqrt(2))*g*i)/2, gh(-1,2,1)},

{a(2), ksi3, pd(a(2,v),v),(mutiplet(-1,2,hig,2,xx2(-1),(h0(0)+xx3(0)*i)/
sqrt(2))*tp(1,2,2,2)*mutiplet(1,2,
hig,2,0,v0/sqrt(2))*g*i-mutiplet(-1,2,hig,2,0,v0/sqrt(2))*tp(1,2,2,2)*mutiplet(1,2,hig,2,xx2(1),
(h0(0)-xx3(0)*i)/sqrt(2))*g*i)/2, gh(-1,2,2)},

{gs(ic10), ksi4 ,pd(gs(ic10,v),v),0, gsg(-1,ic10)}}$

r_ksi_value:=( ksi1 . infinit) (ksi2 . infinit) (ksi3 . infinit) (ksi4 . 1)}$ %Unitary Gauge
```

# Input file for Standard Model at QCD NLO by using onshell scheme

```

%----- Gauge fields -----
gaugefields:=
%No. Name SU(n) notation coupling breaking
'(1 u 1 b g1 yes )
(2 su 2 a g yes )
(3 su 3 gs g3 no ))$
%----- Matter fields -----
matterinput:={{name, 2*spin, chiral, 1, 2, 3},
{hig, 0, rl, 1, 2, 0},
{el, 1, l, -1, 2, 0},
{er, 1, r, -2, 0, 0},
{q1l, 1, l, 1/3, 2, 3},
{q1dr, 1, r, -2/3, 0, 3},
{q1ur, 1, r, 4/3, 0, 3}}$
gauge_boson_redefine:={
a(1,~v) => (w(1,v)+w(-1,v))/2**0.5,
a(2,~v) => (w(-1,v)-w(1,v))/2**0.5/i,
a(3,~v) => z(0,v), b(~v) => p(0,v)};
vancumexpectation:='(hig v0));

% name n_group 1_componet 2_componet ...
mdefl:={ {hig, 2, xx2, (v0+h0-i*xx3)/2**0.5},
{el, 2, nue, ef },
{er, 2, ef },
{q1l, 2, qu, qd },
{q1dr, 2, qd },
{q1ur, 2, qu }}$

realfamily:='( q1l q2l q3l) (q1dr q2dr q3dr)
(q1ur q2ur q3ur) (qu qc qt) (qd qs qb) (el mul tau)
(er mur taur) (ef mu tau) (nue numu nut));

phymass:={{w, wm}, {z, zm}, {p, 0}, {h0, hm},
{ef, fme}, {nue, 0},{mu, fmmu},{numu, 0},{tau, fmtau},
{nut, 0},{qd, fmd}, {qu, fmu},{qs, fms}, {qc, fmc},
{qb, fmb}, {qt, fmt}}$

phyinput:={g3,g,theta,wm, hm,fme, fmmu,fmtau,fmd,
fmu,fms, fmc,fmb, fmt}$

construles:={ g1=>g*sin(theta)/cos(theta)};

expriment_easy_list:={
{g, replaceby, ge, -i*ge*gg(l,v), {p,ef,ef}},
{theta, replaceby, zm} };

charge_def:=tp(2,3)+tp(1,1)/2;

renormalization:='before_broken; %European schem
%renormalization:='after_broken; %Kyoto scheme

ms_list:='(g3 );

symbolic(rform:='(3));
symbolic(rloop:='((g3 . 2)));

```

# Input file for Standard Model at QCD NLO by using MS\_bar scheme

```

%----- Gauge fields -----
gaugefields:=
%No. Name SU(n) notation coupling breaking
'(1 u 1 b g1 yes )
(2 su 2 a g yes )
(3 su 3 gs g3 no ))$
%----- Matter fields -----
matterinput:={{name, 2*spin, chiral, 1, 2, 3},
{hig, 0, rl, 1, 2, 0},
{el, 1, l, -1, 2, 0},
{er, 1, r, -2, 0, 0},
{q1l, 1, l, 1/3, 2, 3},
{q1dr, 1, r, -2/3, 0, 3},
{q1ur, 1, r, 4/3, 0, 3}}$
gauge_boson_redefine:={
a(1,~v) => (w(1,v)+w(-1,v))/2**0.5,
a(2,~v) => (w(-1,v)-w(1,v))/2**0.5/i,
a(3,~v) => z(0,v), b(~v) => p(0,v);
vancumexpectation:='(hig v0));

% name n_group 1_componet 2_componet ...
mdefl:={ {hig, 2, xx2, (v0+h0-i*xx3)/2**0.5},
{el, 2, nue, ef },
{er, 2, ef },
{q1l, 2, qu, qd },
{q1dr, 2, qd },
{q1ur, 2, qu }}$

realfamily:='( q1l q2l q3l) (q1dr q2dr q3dr)
(q1ur q2ur q3ur) (qu qc qt) (qd qs qb) (el mul taul
(er mur taur) (ef mu tau) (nue numu nut));

phymass:={{w, wm}, {z, zm}, {p, 0}, {h0, hm},
{ef, fme}, {nue, 0},{mu, fmmu},{numu, 0},{tau, fmtau},
{nut, 0},{qd, fmd}, {qu, fmu},{qs, fms}, {qc, fmc},
{qb, fmb}, {qt, fmt}}$

phyinput:={g3,g,theta,wm, hm,fme, fmmu,fmtau,fmd,
fmu,fms, fmc,fmb, fmt}$

construles:={ g1=>g*sin(theta)/cos(theta)};

expriment_easy_list:={
{g, replaceby, ge, -i*ge*gg(l,v), {p,ef,ef}},
{theta, replaceby, zm} };

charge_def:=tp(2,3)+tp(1,1)/2;

renormalization:='before_broken; %European schem
%renormalization:='after_broken; %Kyoto scheme

ms_list:='(g3 gs qu qb qt qs qd qc);

symbolic(rform:='(3));
symbolic(rloop:='((g3 . 2)));

```

# Summary



Thanks for your attention!